



$$\text{求 } \iint_S F \cdot \vec{n} dS = \text{其中 } F=(z,-y,x), S:x+2y+2z=2,$$

$$x \geq 0, y \geq 0, z \geq 0$$

$$X(u, v) = (u, v, \frac{2-u-2v}{2})$$

$$X_u = (1, 0, -\frac{1}{2}), X_v = (0, 1, -1)$$

$$E = \frac{5}{4}, F = \frac{1}{2}, G = 2, \vec{n} = (\frac{1}{3}, \frac{2}{3}, \frac{2}{3}), \sqrt{EG-F^2} = \frac{3}{2}$$

$$\iint_S F \cdot \vec{n} dS = \iint_R (\frac{1}{2} - \frac{3}{2}y + \frac{3}{4}x) dx dy = \int_0^1 \int_0^{2-2y} (\frac{1}{2} - \frac{3}{2}y + \frac{3}{4}x) dx dy$$

$$= \int_0^1 (\frac{9}{2}y^2 - 7y + \frac{5}{2}) dy = \frac{1}{2}$$

$$z = f(x, y) = \frac{1}{2}(2-x-2y), \frac{\partial f}{\partial x} = -\frac{1}{2}, \frac{\partial f}{\partial y} = -1$$

$$F \cdot (-\frac{\partial f}{\partial x}, -\frac{\partial f}{\partial y}, 1) = \frac{3}{4}x - \frac{3}{2}y + \frac{1}{2}$$

$$\iint_S F \cdot \vec{n} dS = \iint_R (\frac{3}{4}x - \frac{3}{2}y + \frac{1}{2}) dx dy = \dots$$