

§ Sine Gordon equation

If a surface with  $K=-1$  has first fundamental form written as

$I = \cos^2 \omega du^2 + \sin^2 \omega dv^2$ , then  $\omega$  satisfies the so-called sine-Gordon equation

$$\omega_{uu} - \omega_{vv} = \sin \omega \cos \omega$$